

C.U.SHAH UNIVERSITY

WADHWAN CITY

University (Winter) Examination -2013

Course Name :M.Sc(Physics) Sem-I

Subject Name : -Classical Mechanics

Marks :70

Duration :- 3:00 Hours

Date : 18/12/2013

Instructions:-

- (1) Attempt all Questions of both sections in same answer book / Supplementary.
- (2) Use of Programmable calculator & any other electronic instrument is prohibited.
- (3) Instructions written on main answer Book are strictly to be obeyed.
- (4) Draw neat diagrams & figures (If necessary) at right places.
- (5) Assume suitable & Perfect data if needed.

SECTION-I**Q.1 Write answers of the following Questions**

1. Give the difference between Co-ordinate system and Frame of reference. 2
2. Define Scattering cross-section. 2
3. How the Bertrand's theorem and perturbation of orbits are useful in astronomical units? 2
4. What is the maximum centrifugal acceleration value of earth ? 1

- Q.2 A. Derive the differential equation of orbit. 5
 B. Show that the angular acceleration is the same in Fixed and Rotating frames. 5
 C. Write a note on Virial theorem. 4

OR

- Q.2 A. Derive the Lagrange's equations from Hamilton's principle. 5
 B. Find the equation of orbit and classify different types of orbits on the basis of energy and eccentricity. 5
 C. What is coriolis force? Explain it in brief. 4

- Q.3 A. With the neat diagram discuss the Scattering phenomenon and obtain the expression for differential Scattering cross-section as 7

$$\sigma(\theta) = \frac{1}{4} \left(\frac{z z' b^2}{2E} \right) \text{cosec}^4 \frac{\theta}{2}$$

- B. Derive the Inverse square law of force. 7

OR

- Q.3 A. Discuss Bertrand's theorem with necessary mathematical expression. 7
 B. Using Lagrange's equation for r, obtain the following integral 7

$$t = \int_{r_0}^r \frac{dr}{\sqrt{\frac{2}{m} [E - V(r)] - \frac{l^2}{2mr^2}}}$$

SECTION-II

- Q.4 Write answers of the following Question. 2
1. For Poisson's brackets and prove $[X, X] = 0$. 2
 2. With Example explain stable and unstable equilibrium in small oscillations. 2
 3. If the generating function is $F_2 = q_i p_i$ then prove $p_i = P_i, Q_i = q_i$ and $k = H$. 2
 4. Prove $[u, p_j] = \frac{\partial u}{\partial q_j}$ 1



Q.5 A. For small oscillations obtain Lagrange's equation as 5

$$\sum_j T_{jk} \ddot{q}_j + \sum_j V_{jk} q_j = 0$$

What are V_{jk} and T_{jk} ?

B. What are normal co-ordinates? Explain briefly. 5

C. Explain Gauge transformation. 4

OR

Q.5 A. Discuss the Eigen Vectors and Eigen Frequencies using two coupled pendulum. 5

B. Give the Example of Harmonic Oscillator. 5

C. Define the Poisson's brackets and prove the following 4

$$[\{p_j, H\}, H] = -\dot{p}_j$$

Q.6 A. What is Canonical transformation ? Obtain the transformation equation for generating function F_1 . 7

B. Derive Hamilton-Jacobi equation and obtain its solution. 7

OR

Q.6 A. Derive expressions for Small Oscillations of particle on string. 7

B. Obtain Hamilton's characteristics function and find the relation in which the time is as a co-ordinate and Hamiltonian is its conjugate momentum. 7

